

## SOF INTERNATIONAL MATHEMATICS OLYMPIAD 2023-24



## DO NOT OPEN THIS BOOKLET UNTLL ASKED TO DO SO

Total Questions: 50 | Time: 1 hr.

## Guidelines for the Candidate

1. You will get additional ten minutes to fill up information about yourself on the OMR Sheet, before the start of the exam.
2. Write your Name, School Code, Class, Section, Roll No. and Mobile Number clearly on the OMR Sheet and do not forget to sign it. We will share your marks / result and other information related to SOF exams on your mobile number.
3. The Question Paper comprises four sections:

Logical Reasoning (15 Questions), Mathematical Reasoning (20 Questions), Everyday Mathematics (10 Questions) and Achievers Section (5 Questions)
Each question in Achievers Section carries 3 marks, whereas all other questions carry one mark each.
4. All questions are compulsory. There is no negative marking. Use of calculator is not permitted.
5. There is only ONE correct answer. Choose only ONE option for an answer
6. To mark your choice of answers by darkening the circles on the OMR Sheet, use HB Pencil or Blue / Black ball point pen only. E.g. Q.16: Rahul bought 4 kg 90 g of apples, 2 kg 60 g of grapes and 5 kg 300 g of mangoes. The total weight of all the fruits he bought is $\qquad$ -.
A. 11.450 kg
B. 11.000 kg
C. 11.350 kg
D. 11.250 kg

As the correct answer is option A, you must darken the circle corresponding to option A on the OMR Sheet.
16.
(B) (C) (D)
7. Rough work should be done in the blank space provided in the booklet.
8. Return the OMR Sheet to the invigilator at the end of the exam.
9. Please fill in your personal details in the space provided before attempting the paper.

Name: $\qquad$

SOF Olympiad Roll No. $\qquad$ Contact No. $\qquad$

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## LOGICAL REASONING

1. Three different positions of a cube are shown below. Which of the following alphabets will be on the face opposite to the face having alphabet M?

A. L
B. N
C. Q
D. $R$
2. Select the odd one out.
A. JMPS
B. FILO
C. BEGJ
D. QTWZ
3. If '*' denotes ' $x$ ', ' $\#$ ' denotes ' + ', ' $\%$ ' denotes ' - ' and ' $\$$ ' denotes ' $\div$ ', then which of the following equations is incorrect?
A. $5 \# 6 \$ 3 * 4 \% 9=4$
B. 5 * $9 \$ 3 \# 4 \% 6=13$
C. $5 \# 3 * 6 \$ 2 \% 8=10$
D. $5 * 6 \$ 3 \# 4 \% 8=6$
4. Which of the following options will complete the pattern in the given figure?

A.

B.

C.

A. 15
B. 17
C. 20
D. 18
5. Which of the following options does not satisfy the same conditions of placement of the dots as in the given figure?

A.

B.

C.

D.

6. Pointing to a girl in a party, Gopal said, "She is the daughter of my son's wife." How is that girl related to Gopal?
A. Grandmother
B. Aunt
C. Granddaughter
D. Daughter-in-law
7. Count the number of squares formed in the given figure.

A. 11
B. 12
C. 13
D. More than 13
8. Anusha comes out of her school and walks 50 m towards East. She then turns right and walks 20 m .

Now, she turns left and walks 20 m . She again turns right and walks 50 m to reach her home. In which direction is her home from the school?
A. North
B. South-West
C. North-West
D. South-East
12. Select the correct water image of the given figure.
A.

B.

C.

D.

13. If 'METAL' is coded as ' 72856 ' and 'MIND' is coded as '7341', then how will 'DILEMMA' be coded in that code language?
A. 7362115
B. 1362775
C. 1328776
D. 7352775
14. Which of the following Venn diagrams best represents the relationship amongst, 'Mothers, Brothers and Parents'?
A.

B.

C.

D.

15. Select a figure from the options which will complete the given figure matrix.

A.

B.

C.

D.


## MATHEMATICAL REASONING

16. Solve:
$3 \frac{1}{7}+\left(\frac{-5}{14}\right)+\left(\frac{-7}{12}\right)+2 \frac{3}{4}$
A. $-7 \frac{1}{20}$
B. $4 \frac{20}{21}$
C. $3 \frac{5}{21}$
D. None of these
17. How many of the following expressions are binomials? $5 a^{2}+3 b, 2 a+3 b, 8 a^{2}, 9 a^{2}+5 a+3 b^{2}, 7 a b+3 a^{2}$
A. 3
B. 2
C. 4
D. 5
18. Which of the following statements is CORRECT?
A. All natural numbers are whole numbers and all whole numbers are integers.
B. All whole numbers are integers and all integers are natural numbers.
C. All integers are whole numbers and all natural numbers are integers.
D. All integers are whole numbers and all integers are natural numbers.
19. How many distinct prime factors does the smallest 5 -digit number has?
A. 2
B. 3
C. 4
D. 5
20. Which of the following options shows the top view of the given figure?

A.

B.

C.

D.

21. In the given figure (not drawn to scale), if $l \| m$, then find the value of $a+b$.

A. $153^{\circ}$
B. $59^{\circ}$
C. $124^{\circ}$
D. $79^{\circ}$
22. Find the value of $\frac{(-4)^{5} \times(-3)^{4}}{(-4)^{3} \times(-4)^{2}}+\left[\left\{\left(\frac{3}{4}\right)^{2}\right\}^{3}\right]^{0}$.
A. -4
B. 27
C. 82
D. None of these
23. Which of the following equations is correct for the statement given below?
"The sum of one-seventh, one-third and one-fourth of a number $m$ exceeds the same number by 10 ."
A. $\frac{m}{7}+\frac{m}{3}+\frac{m}{4}=10-m$
B. $\frac{m}{7}+\frac{m}{3}+\frac{m}{4}=m+10$
C. $\frac{m}{7}+\frac{m}{3}+\frac{m}{4}=10$
D. $\frac{m}{7}+\frac{m}{3}+\frac{m}{4}+10=m$
24. Find the value of $x, y$ and $z$ in the given figure (not drawn to scale).

A. $x=40^{\circ}, y=30^{\circ}, z=50^{\circ}$
B. $x=20^{\circ}, y=30^{\circ}, z=80^{\circ}$
C. $x=20^{\circ}, y=20^{\circ}, z=80^{\circ}$
D. $x=30^{\circ}, y=40^{\circ}, z=60^{\circ}$
25. If $11 \frac{5}{21}$ is subtracted from $15 \frac{3}{14}$ and the difference is multiplied by 504 , then what will be the result?
A. 2024
B. 2104
C. 2004
D. 2014
26. Two numbers are in the ratio $2: 3$. If 2 is subtracted from the smaller number and 6 is subtracted from the greater number, then the ratio becomes $3: 4$. Find the sum of the two numbers.
A. 50
B. 38
C. 45
D. 25
27. The simple interest on a sum of money is $\frac{4}{9}$ of the principal. Find the rate percent and time, if both are numerically equal.
A. $5 \frac{2}{3} \%, 5$ years 8 months
B. $7 \frac{2}{3} \%, 7$ years 8 months
C. $6 \frac{2}{3} \%, 6$ years 8 months
D. $6 \frac{2}{3} \%, 7$ years 8 months
28. What is the least number which when decreased by 4 is exactly divisible by each of the numbers 10,15 , 20 and 25 ?
A. 304
B. 296
C. 354
D. 350

Direction (29-30): The given double bar graph shows the number of people who like five different brands. Study the graph carefully and answer the following questions.

29. What percent of total males like brands $R$ and $T$ together?
A. $45 \frac{2}{3} \%$
B. $40 \frac{5}{8} \%$
C. $31 \frac{1}{3} \%$
D. None of these
30. Find the ratio of number of males who like brands $P$ and $Q$ together to the number of females who like brands $S$ and $T$ together.
A. $5: 12$
B. $17: 10$
C. $10: 17$
D. $12: 5$
31. Which of the following statement(s) is/are true?
(i) Order of rotational symmetry of an equilateral triangle is 3.
(ii) The number of lines of symmetry of a regular hexagon is 5 .
A. Only (i)
B. Only (ii)
C. Both (i) and (ii)
D. Neither (i) nor (ii)
32. Which of the following is not equal to $24.675 \times 3.489$ $\times 0.735$ ?
A. $2467.5 \times 34.89 \times 0.000735$
B. $0.24675 \times 3489 \times 0.0735$
C. $0.24675 \times 0.3489 \times 735$
D. $2.4675 \times 3.489 \times 73.5$
33. What should be subtracted from the greatest 6 -digit number that can be formed by using the digits 5,3 , 6,8 and 4 (each digit at least once) to get 100000 ?
A. 766543
B. 582614
C. 786543
D. None of these
34. How many acute angles are there in the given figure?

A. 6
B. 5
C. 7
D. More than 7
35. A sum of money invested at simple interest becomes $₹ 306$ at the end of 5 years. If the interest is $\frac{9}{25}$ th part of the principal, then what is the rate of interest per annum?
A. $7 \frac{1}{5} \%$
B. $9 \frac{1}{5} \%$
C. $7 \frac{5}{7} \%$
D. $7 \frac{2}{5} \%$

## EVERYDAY MATHEMATICS

36. In a game, team $P$ scored $-40,10,50,-20,15$ points and team $Q$ scored $40,-20,-10,30,20$ points in five consecutive rounds. Which team scored more points and by how much?
A. $P, 30$ points
B. $\mathrm{Q}, 40$ points
C. $\mathrm{Q}, 45$ points
D. $P, 25$ points
37. A rectangular piece of land is to be sold off in smaller pieces. The total area of the land is $2^{17} \mathrm{sq}$. miles. Each piece to be cut out is $16^{2}$ sq. miles in size. How many smaller pieces of the land can be sold at the given size?
A. $2^{15}$
B. $16^{4}$
C. $2^{9}$
D. None of these
38. Megha is 20 years younger to her mother. After 10 years, her mother will be twice as old as Megha. Find the present age of Megha.
A. 15 years
B. 12 years
C. 10 years
D. 18 years
39. The floor of a room 3 m long and 1.5 m wide is to be covered with the tiles each of size 12 cm by 5 cm . Find the cost of covering the floor with tiles at the rate of $₹ 5$ per tile.
A. ₹ 3150
B. ₹ 2250
C. ₹ 2950
D. ₹ 3750
40. Out of 6 types of ice creams, Sneha wants to purchase the chocolate ice cream which is most liked by the children. Which measure of central tendency would be most appropriate, if the data is provided to her?
A. Mean
B. Median
C. Mode
D. Range
41. Manish starts a journey. After travelling some distance, he finds that $\frac{4}{7}$ of the journey is covered and still he has to cover 150 km . How long was the total journey?
A. 200 km
B. 280 km
C. 350 km
D. 420 km
42. A fruit seller bought 20 kg apples at ₹ 6 per kg and 30 kg apples at ₹ 7 per kg . At what rate per kg should he sell them to gain $30 \%$ ?
A. ₹ 7.50
B. ₹ 9.25
C. ₹ 8.58
D. None of these
43. From his home, Rahul walks $\frac{6}{7} \mathrm{~km}$ towards school and then returns $\frac{5}{6} \mathrm{~km}$ on the same way towards his home to reach a landmark. At what distance will he be now from his home?
A. $\frac{1}{42} \mathrm{~km}$
B. $\frac{1}{43} \mathrm{~km}$
C. $\frac{30}{42} \mathrm{~km}$
D. $\frac{11}{42} \mathrm{~km}$
44. Priyanka's monthly income is ₹ 85000 . She pays $7 \frac{1}{2} \%$ of it as house rent and $20 \%$ of the remaining amount on her child's education. How much total money is left with her?
A. ₹ 51500
B. ₹ 62900
C. ₹ 47400
D. None of these
45. A shopkeeper sold $3152.50 \mathrm{~kg}, 2905.75 \mathrm{~kg}$ and 1554.18 kg of wheat on three consecutive days. How much total quantity of wheat he sold in the given three days?
A. $\quad 7612.43 \mathrm{~kg}$
B. $\quad 7928.62 \mathrm{~kg}$
C. 5418.18 kg
D. $\quad 6719.48 \mathrm{~kg}$

## ACHIEVERS SECTION

46. Fill the table and find the value of $Q-2 P-R$.

|  | Number <br> of edges | Number <br> of faces | Number <br> of vertices |
| :---: | :---: | :---: | :---: |
|  | $Q$ | $P$ | 4 |
|  | 10 | 6 | 12 |

A. 4
B. 5
C. 18
D. None of these
47. Read the given statements carefully and state $T$ for true and F for false.
(i) The value of $(-71-(-45)) \times(70-50)+400$ is -120 .
(ii) -78 should be subtracted from the product of 15 and -8 to get -198 .
(iii) The value of $a+(b+c)-(a+b)+c$ for $a=5, b=-2$ and $c=3$, is 0 .

|  | (i) | (ii) | (iii) |
| :---: | :--- | :---: | :---: |
| A. | F | T | F |
| B. | T | F | F |
| C. | T | F | T |
| D. | F | F | T |

48. Read the given statements carefully and select the correct option.
Statement-I : If the median of the observations $15,17,20,20,24, a+5,29,31,31,33,34$ (arranged in ascending order) is 27 , then the mean of the above data is 20 .

Statement-II : The median and mode of the given data, $70,52,47,64,47,71,58$ are 58 and 47 respectively.
A. Both Statement-I and Statement-II are true.
B. Statement-I is true but Statement-II is false.
C. Both Statement-I and Statement-II are false.
D. Statement-I is false but Statement-II is true.
49. Solve the following :
(i) An article passing through two hands is sold at a profit of $38 \%$ at the original cost price. If the first dealer makes a profit of $20 \%$, then find the profit percent made by the second dealer.
(ii) In an office of 125 employees, 15 are absent, $10 \%$ of the remaining have failed to achieve the target. Find the number of employees who achieve their target.

|  | (i) | (ii) |
| :--- | :--- | :--- |
| A. | $15 \%$ | 90 |
| B. | $10 \%$ | 88 |
| C. | $15 \%$ | 99 |
| D. | None of these |  |

50. Fill in the blanks and select the correct option.
(i) The value of $\left(\frac{-28}{81} \div \frac{14}{27}\right)+\left(\frac{-3}{4}\right)$ is $\mathbf{P}$.
(ii) If $x=\frac{3}{2}+\frac{9}{8}$ and $y=\left(\frac{-9}{16}\right) \times\left(\frac{-5}{18}\right) \times 4 \frac{4}{5}$, then the value of $\frac{x+y}{x-y}$ is $\qquad$ Q -
(iii) On subtracting the quotient of $\left(\left(\frac{-5}{9}\right) \div \frac{1}{18}\right)$ from the quotient of $\left(\frac{9}{5} \div\left(\frac{-3}{5}\right)\right)$, we get $\underline{\mathbf{R}}$.

| $\mathbf{P}$ | $\mathbf{Q}$ | R |
| :--- | :--- | :--- |

A. $\frac{-1}{17}$
$\frac{-5}{9}$
R
$\frac{-1}{7}$
B. $\frac{-17}{12}$
$\frac{9}{5}$
C. $\frac{3}{19}$
$\frac{4}{5}$
$\frac{-1}{8}$
D. $\frac{-17}{12}$
$\frac{4}{5}$8

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